#### Mediation and Moderation 101

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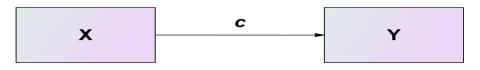
November 10, 2021

#### Goals of Today's Talk

- Introduce the concept of statistical mediation and methods for assessing mediation.
- Introduce the concept of statistical moderation, types of moderation, and limitations of moderation analyses.
- Apply these concepts to example CADC scientist models (redacted for posting on the web).
- Today's talk will not provide in-depth guidance on how to perform mediation and moderation analyses and how to interpret results from those analyses (but will point to resources to learn more about mediation and moderation analyses, including how to do them).

#### What is statistical mediation?

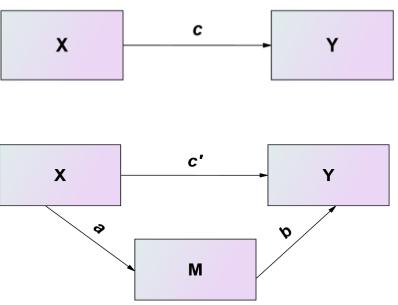
 Consider an exposure X and an outcome Y. A typical research question might ask, "What is the effect of X on Y?" or "Does X affect Y significantly?" Visually, this relationship can be depicted this way:



- *c* is the *total effect* of X on Y.
- But what if we thought X affected something else that in turn affected Y that could explain the X->Y association?

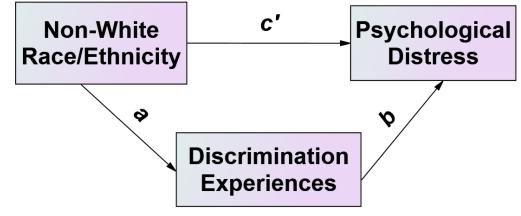
# Mediation (Sequential)

- We introduce a new variable, M, that is caused by X and in turn causes Y. We implicitly assume that X precedes M and M precedes Y (temporal ordering).
- **c'** is the *direct effect* of X on Y.
- *a* is the direct effect of exposure X on the mediator M.
- **b** is the direct effect of the mediator M on the outcome Y.
- This model is known as a sequential mediation model.
- Let's look at a hypothetical example to help make these principles more concrete.



#### Sequential Mediation Example

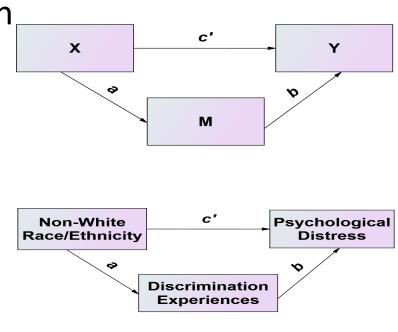
- To make this concrete, imagine a simplified example based on Scheim and Bauer (2019).
- Scheim and Bauer were interested in whether experiences of discrimination mediated an association between non-White race/ethnicity and psychological distress.



 In other words, could people's experiences of discrimination explain or account for a previously observed link between non-White race/ethnicity and distress?

#### Mediation 1.0: Four Causal Steps

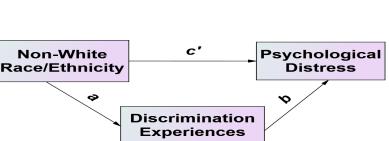
- Mediation 1.0: The first mediation approaches developed in the 1980s used a series of linear regression models to estimate mediation effects (Baron & Kenny, 1986).
- <u>Step 1</u>: Estimate the *direct effect* of X on M (*a*). E.g., the effect of race/ethnicity on discrimination.
- <u>Step 2</u>: Estimate the *total effect* of X on Y (*c*). E.g., the effect of race/ethnicity on psychological distress.



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#### Mediation 1.0: Causal Steps Three & Four

- <u>Step 3</u>: Estimate the direct effect of X (**c'**) and M (**b**) on Y. E.g., the effects of race/ethnicity and discrimination on distress.
- <u>Step 4</u>: Assess mediation by examining **a**, **b**, **c** and **c'**:
- The direct effects X on M (a) and M on Y (b) must be significant.
  E.g., race/ethnicity must significantly affect discrimination and discrimination must affect distress.



c'

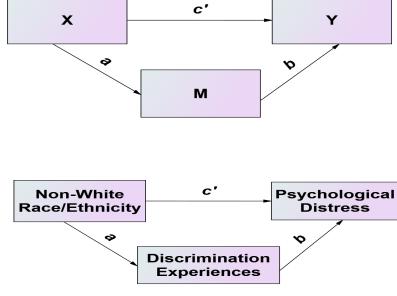
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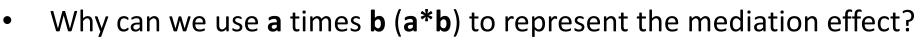
#### Assessing Mediation 1.0: Causal Steps

- If the total effect *c* from the X->Y model is significant, but the direct effect *c*' from X+M->Y model is non-significant, then it is concluded that M *completely mediates* the X->Y association.
- On the other hand, if the total effect *c* from X->Y is significant and the effect *c*' from the X+M->Y model is also significant, then it is concluded that M *partially mediates* the X->Y association.
- In our example, the total effect of X on Y is race/ethnicity -> psychological distress in a model without its mediator included.
- Some methodologists (e.g., Hayes & Rockwood, 2017) view the distinction between partial vs. full mediation as being outdated.



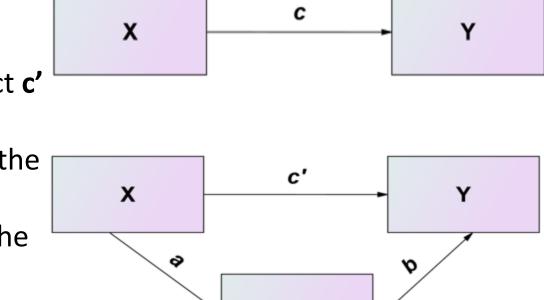
# **Assessing Mediation: Indirect Effect**

- How can we quantify the mediation effect?
- Intuitively, we could subtract c' from c. I.e., subtract the direct effect of X on Y from the total effect (difference method). What remains is the mediation effect.
- Or we could multiply a times b (product method) instead.



In linear regression, the total effect of X on Y can be decomposed into c = a\*b + c'. Thus, c – c' = a\*b, which is the effect of mediation. It is often referred to as the *indirect effect* of X on Y through M.

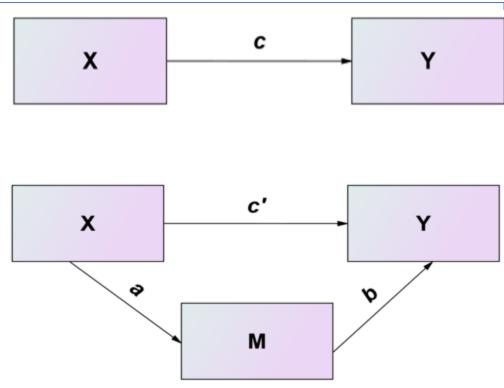




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#### Indirect Effect Via a\*b

- For logistic, multilevel, and other models, a\*b only approximately equals c – c', so a\*b is more often used to quantify the indirect effect than c – c'. (Kenny, 2021).
  - There are several methods for testing the significance of the a\*b indirect effect. See slide 29 of S. Gregorich's (2014a) mediation talk.



 Since indirect effects are products of a and b and thus often asymmetrically distributed, asymmetric confidence intervals are best for making inferences about the significance of indirect effects.

#### Mediation 2.0: Structural Equation Modeling (SEM)

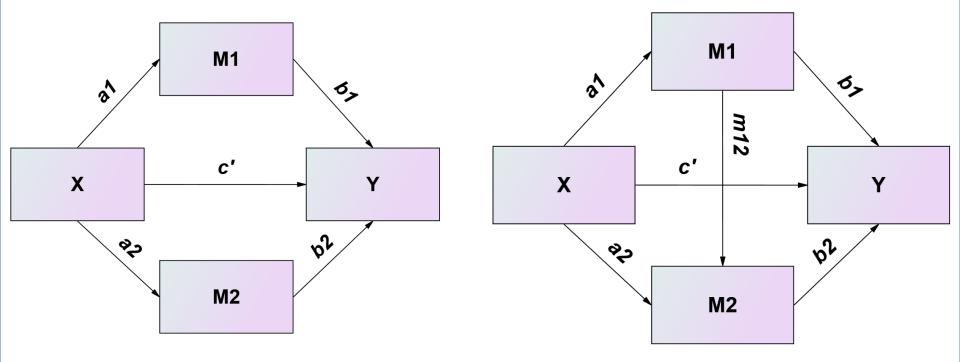
- According to Tyler VanderWeele, an international expert on mediation analysis, the Baron & Kenny (1986) causal steps paper has been cited over 90,000 times. This seminal paper's impact on many fields had been profound and undeniable. One way to frame their causal steps approach is as mediation version 1.0.
- However, the regression-based causal steps method has some limitations. For instance, the sample is assumed to be the same for all three regression models; missing data in real-world applications can challenge this assumption.
- Thus, in the 1990s, structural equation modeling (SEM) became popular for testing mediation. SEM is a *simultaneous equation estimation method*, meaning that it can estimate all pathways simultaneously. We could view this SEM approach to mediation analysis as mediation version 2.0. What are its advantages?

#### Mediation via SEM: Advantages

- Full-information maximum likelihood estimation (FIML) can address missing data, which resolves the problem of different Ns for the various regression equations in the causal steps approach.
- Most specialty SEM programs (or SEM commands in general stats packages like Stata) can easily compute the **a\*b** indirect effects as well as their asymmetric confidence intervals via bootstrapping.
- Latent variables can represent shared variance among multiple correlated variables for X, M, and/or Y. This is particularly helpful for M because it can reduce the impact of measurement error. By reducing measurement error, accuracy and statistical power are maximized for testing indirect effects (Hoyle and Kenny, 1999).
- Biggest advantage: A much broader array of models may be specified, including models with multiple mediators.

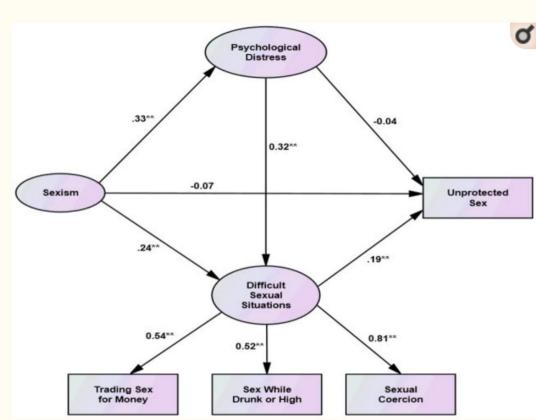
#### **SEM-Based Mediation Examples**

• SEM can be used compute total, direct, and indirect effects seamlessly, including for multiple mediator models like these:



#### Example of "Chained" Mediation

- Choi, Bowleg, and Neilands (2011) fitted a mediation model with a latent difficult sexual situations variable measured by three correlated indicators.
- The model revealed a "chain" of mediation from women's experiences of sexism through psychological distress to difficult sexual situations leading to unprotected sex.
- Sexism also affected unprotected sex through difficult sexual situations.



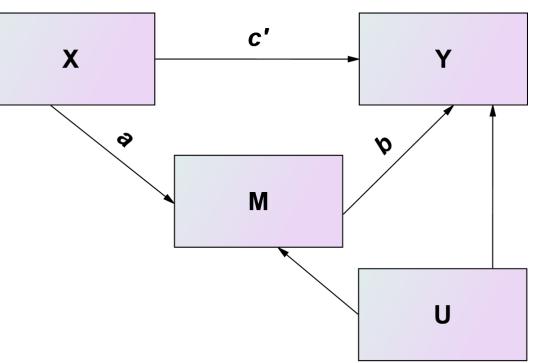
#### FIGURE 1

Hypothesized Structural Equation Model for Any Unprotected Sex with a Primary Sexual Partner: Standardized Path Weights (N=754)\* p < 0.05; \*\* p < 0.01

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#### **Classical Regression and SEM limitations**

- Traditional regression and SEM-based mediation analyses rely on some fairly strong assumptions.
- First, even if participants were randomly assigned to the exposure X or if all possible exposureoutcome confounders were controlled for, there may be still be mediatoroutcome confounding (U) because participants are typically not randomly assigned to M.
- U might represent one or many variables, observed or unobserved.



#### More Limitations and a Remedy

- Uncontrolled confounders can bias mediation analysis effect results.
- Another limitation of the traditional regression and (most) SEM-based approaches is their assumption of no interaction between (a) the exposure X and the mediator M and (b) no interactions of X and M with other potential confounders. Ideally, we would like to be able to investigate and account for such interactions if any are present.
- Finally, while some ad hoc methods have been advanced for noncontinuous M and Y variables, it would be helpful to have a general framework that allows for non-continuous M and/or Y variables.
- Causal mediation methods address these issues. They extend traditional regression and SEM-based methods to allow noncontinuous M and Y variables and they also allow interactions.
  - See Valeri and Vanderweele (2013) for an introduction and SAS & SPSS macros. SAS PROC CAUSALMED, the Stata -paramed- user-written command, and various R commands are also available (Valente et al, 2020)

# Mediation 3.0: Causal Mediation

- *Causal mediation* methods take a different approach from traditional mediation methods.
- Rather than focus on parameter estimates from parametric regression models, causal mediation invites us to consider a thought experiment.
- In an ideal experiment, we would like to randomize everyone to an exposure X at level 0 of X (e.g., control) and level 1 of X (e.g., intervention).
- Assuming an outcome Y, we would also ideally like to be able to observe the value of Y at X=0 (Y(0)) and X=1 (Y(1)).
- But in reality, we can only randomize a given individual to X=0 **or** X=1, not both. Thus, if someone was randomized to X=0 (or observed at X=0 in a non-randomized study), Y(0) is an observable outcome, but Y(1) is an unobservable *potential outcome* or *counterfactual* and vice versa for X=1.
- However, averaging across all study participants, we can compute a treatment effect as E[Y(1)-Y(0)].
- We can compute this same effect at different levels of a mediator M.

#### **Causal Mediation Effects**

- There are six causal mediation effects (Valente et al, 2020). Main five:
- Total natural indirect effect (TNIE):
  - TNIE = E[Y(1,M(1)) Y(1,M(0))]: The effect of X on Y through M when the direct effect is held constant at the treatment level X=1
- Pure natural indirect effect (PNIE):
  - PNIE = E[Y(0,M(1)) Y(0,M(0))]: The effect of X on Y through M when the direct effect is held constant at the control level X=0
- Total natural direct effect (TNDE):
  - TNDE = E[Y(1,M(1)) Y(0,M(1))]: The effect of X on Y when the mediation effect is held constant at its naturally observed treatment level M=1
- Pure natural direct effect (PNDE):
  - PNDE = E[Y(1,M(0)) Y(0,M(0))]: The effect of X on Y when the mediation effect is held constant at its naturally observed control level M=0
- The total effect of X on Y (TE):
  - E[Y(1,M(1)) Y(0,M(0))] = TNDE + PNIE = PNDE + TNIE

#### Causal Mediation: CDE and More

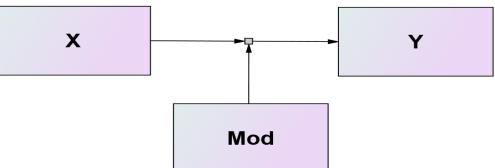
- The sixth causal mediation effect is less frequently used. It is the controlled direct effect (CDE), which is defined as the effect of X on Y at some fixed value of M of substantive interest.
  - CDE = E[Y(1,m) Y(0,m)] where m is a fixed value of M
- The CDE may be most useful for answering "what if" policy-type questions: E.g., "If we changed the value of the mediator M to m, what would the effect of X on Y be?" m needs to be set to a meaningful value.
- Causal mediation methods generally assume no unobserved confounding of the X->Y, X->M, and M->Y relationships.
- Causal mediation methods allow for inclusion of observed confounders. The causal mediation literature proposes sensitivity analysis methods to evaluate whether any remaining uncontrolled confounding is an issue.
- For an extensive "deep dive" into causal mediation, see VanderWeele (2015) and his numerous articles.

# Additional Mediation Considerations

- When designing your studies consider the following: If you can randomize *both* X and M, that will enable you to make the strongest possible causal inferences. For instance, the multiphase optimization strategy (MOST) method randomizes participants to receive various subcomponents of a combination intervention using a factorial design to help tease apart which parts of the intervention worked rather than relying on a post-hoc mediation analysis (see Collins et al, 2007).
- It is unusual to be able to randomize M, however, so at the study design stage, carefully consider potential confounders of X->Y, X->M, and X->Y and plan to measure them whenever possible.
- It is also important to consider the timing of mediation (i.e., when to measure mediators). Subject-matter knowledge is important.
- Cross-sectional analyses of X->M->Y may yield biased results (Mitchell & Maxwell, 2013). Some reviewers and journals will accept crosssectional mediation results (with stated limitations) but others will not.

#### Moderation

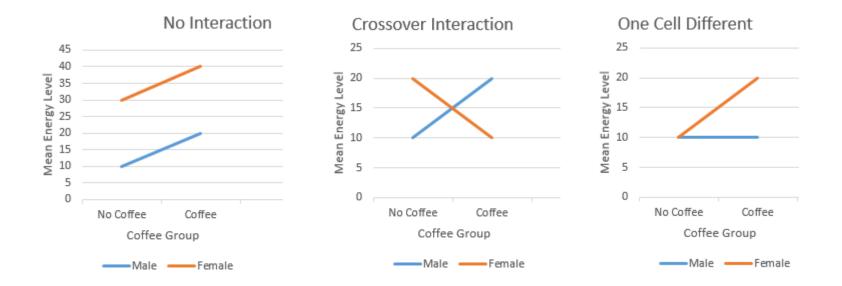
- Moderation occurs when the effect of one variable on another, say X on Y, is changed by a third variable "Mod" (e.g., race/ethnicity).
- Moderation is sometimes called *effect modification* by epidemiologists and public health researchers and *statistical interaction* by biostatisticians (Gregorich, 2014b).
- The moderator "Mod" can be continuous or binary. The diagram at right contains a shorthand representation of a regression model with Y explained by X, Mod, and an X-by-Mod interaction term.



• A limitation: Typically, many more participants are required to have good power to test for interaction effects relative to testing main effects.

#### **Interaction Patterns**

• There can be different *patterns* of interactions (see Gregorich, 2014b slides 4-7)). Here are a few examples:



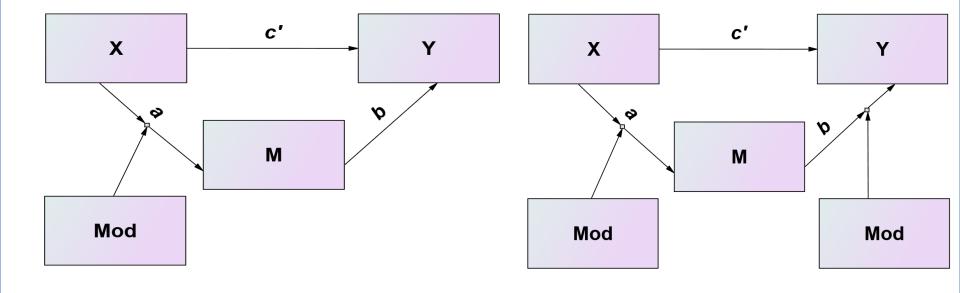
- There are other possibilities, especially when there are more than two levels of each factor or if one or both predictors are continuous.
- General rule: If the lines are not parallel, there is interaction present. Conversely, if the lines are parallel, there is no interaction present.

#### **Types of Interactions**

- The most commonly-specified type of interaction is a *multiplicative interaction* in which X and Mod are multiplied to yield a product term that is included in the model along with the X and Mod main effects.
- When Y is continuous, a test of the X\*Mod multiplicative interaction will yield identical results to comparing the means directly at different levels of X and Mod (i.e., difference of means = mean of differences).
- When Y is not continuous (e.g., binary), that equivalence no longer holds. Thus, epidemiologists and public health researchers with binary outcome variables are increasingly interested in *additive interactions*. An additive interaction is an interaction studied on the probability scale rather than on the log-odds or log-risk scale. See VanderWeele & Knol (2014) for an in-depth published tutorial on this topic and Wall (2013) for a readable online introductory slide deck.

# **Combining Moderation and Mediation**

- It is possible to combine moderation and mediation in the same analysis (Fairchild et al, 2009).
- Mediated moderation occurs when an interaction (i.e., moderation) effect is mediated by a mediator (first diagram below [left side]).
- Moderated mediation occurs when an indirect (i.e., mediation) effect is modified by another variable (second diagram below [at right])



#### Resources

- Gregorich 2014(a) and 2014(b) are available on the CADC website. These two presentations provide introductory yet more in-depth coverage of (non-causal) mediation and moderation, respectively.
- Causal mediation software comparative review article (with clear definitions of the causal mediation effects): Valente et al (2020)
- To learn more about causal mediation methods, consult Valeri and VanderWeele (2013). Dr. VanderWeele also has tools and free video links to a day-long course taught in 2015 on his web site: <u>https://www.hsph.harvard.edu/tyler-vanderweele/tools-and-tutorials/</u>.
- For the most up-to-date training, Dr. VanderWeele also teaches an excellent short course on causal mediation for Statistical Horizons: <u>https://statisticalhorizons.com/causal-mediation-analysis</u>. The course is taught in an on-demand format (self-paced recorded lectures over a 4-week period with a Q&A forum on Slack) with software demonstrations conducted in SAS and Stata. It will be offered next May.

#### Conclusions

- Study design: Consider options for randomly assigning mediators as well as exposures (e.g., MOST). When incorporating non-randomized mediators, consider measurement timing and measuring confounders.
- Moderation tests require a lot more participants to achieve satisfactory power for detecting effects (e.g., 4x or more; e.g., Leon & Heo, 2009).
  - One corollary implication is that if you are planning to test moderation by race/ethnicity (or another categorical variable), you will need sufficient *n* for the various race/ethnicity groups you are studying.
  - For these reasons, proposed moderation analyses are often exploratory.
- For sequential X->M->Y models, consider causal mediation methods, especially if you have non-continuous M and/or Y variables and/or interactions, especially exposure-mediator interactions.
- For multiple-mediator models, SEM can be an accessible approach, with limitations. Stay tuned for new accessible causal-based options for multiple mediator and longitudinal models as they become available.

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